

TM No. 316-489-76

ADA U83556

NAVAL UNDERWATER SYSTEMS CENTER NEW LONDON LABORATORY NEW LONDON, CONNECTICUT 06320

Technical Memorandum

A NEARFIELD MODEL OF THE PARAMETRIC BADIATOR PART III CONVOLUTION METHOD

DTC ELECTE APR 2 8 1980

NILL HOLL

19 October 1976

Prepared by:

R. H./Mellen Advanced Systems Technology Division

M. B. Moffett,
Sonar Transducers and
Arrays Division

\* To be presented at the 93rd meeting of the Acoustical Society of America, University Park, Pennsylvania, June 1977.

Approved for public release; distribution unlimited.

80 4 28 008

4105116.

ゴベルン

TM No. 316-489-76

# **ABSTRACT**

The line array solution of Part I is used in convolution with the primary pattern to calculate the field of collimated and spherically diverging sources of arbitrary transverse distribution.

# ADMINISTRATIVE INFORMATION

This memorandum was prepared under NUSC Project A61400, "Nearfield Model for Parametric Acoustic Sources", Principal Investigator, R. H. Mellen; Associate Investigator, M. B. Moffett; and Program Manager, J. H. Probus MAT 035.

The authors of this memorandum are located at the New London Laboratory, Naval Underwater Systems Center, New London, CT 06320.

A

# INTRODUCTION

In Part I (reference (1)) the contour integration method was used to calculate the field of a line array. On the axis the solution has a logarithmic singularity. Finite aperture axial levels were calculated for two special cases: a cylindrical and a conical source in which the transverse densities are constant within the aperture and zero outside. A "complete" field solution for each case is now obtained in which the transverse distributions can be arbitrary. The solution is in the form of a convolution between the line array pattern and the source pattern. This is equivalent to summing the fields of a bundle of line arrays of appropriate weights.

### CYLINDRICAL SOURCE

The volume integral for the cylindrical source can be written

$$\psi(R) = \frac{Q_0 \exp(-\alpha L - ikL)}{4\pi} \int_0^{2\pi} d\gamma' \int_0^{\infty} a' da' D(a', \gamma') \int_{-L}^{\infty} \frac{dx \exp\left[-2\alpha x - ik(\sqrt{x^2 + a_1^2} + x)\right]}{\sqrt{x^2 + a_1^2}}$$
(1)

Where  $\psi$  is the velocity potential,  $Q_0$  is the linear source density, R is the range vector to the field point and  $a_1^2 = a^2 + a'^2 - 2aa' \cos(\gamma' - \gamma)$  where  $\gamma'$  is the cylindrical angle of the radius a'.  $D(a', \gamma')$  is the normalized transverse distribution function; i.e.

$$\int_0^{2\pi} d\gamma' \int_0^{\infty} a' da' D(a',\gamma') = 1$$
 (2)

Let Y = L  $\psi$ (L,a)exp(ikL)/S<sub>0</sub> where S<sub>0</sub> = Q<sub>0</sub>/4 $\pi\alpha$  is the Westervelt source strength. Equation (1) can then be written in dimensionless form as

$$Y = \int_{0}^{2\pi} d_{\gamma}' \int_{0}^{\infty} a' da' D(a'_{3\gamma}') Y(u_{0}, v_{0})$$
 (3)

From reference (1)

$$Y(u_0, v_0) = u_0 \exp(-u_0) \int_{z_0}^{\infty} \frac{dz \exp(-z)}{\sqrt{z^2 + B^2}}$$
 (4)

is the line array solution and where  $z + -u_0 + iv_0 = -2\alpha L + ika_1^2/2L$  and  $B^2 = 4iu_0v_0$  for L>>a.

Equation (4) is easily evaluated along the contour  $z = t - u_0 + iv_0$ . Equation (3) is then the two dimensional convolution of Equation (4) and  $D(a',\gamma')$ .

# **DIVERGING SOURCE**

In the spherical case let  $Y = R\psi(R) \exp(ikR)/S_0$ . Equation (3) becomes

$$Y = \int_0^{2\pi} d\gamma' \int_0^{\pi} d\phi' \sin\phi' D(\phi',\gamma') \exp(iv_0) Y(u_0,v_0)$$
 (5)

where D is the normalized density function; i.e.

$$\int_{0}^{2\pi} d\phi' \sin\phi' D(\phi',\gamma') \equiv 1$$
 (6)

and where  $Y(u_0,v_0)$  is again given by Equation (4). For small angles  $u_0 = 2\alpha R$ ,  $v_0 = u_0\theta_1^2$  and  $\theta_1^2 = \theta^2 + \theta^{'2} - 2\theta\theta^{'}\cos(\gamma^{'}-\gamma)$  where  $\theta^{'} = \phi^{'}/\phi_0$ ,  $\phi_0$  being the characteristic Westervelt angle of reference (1). At long ranges  $Y(u_0,v_0)$  approaches the Westervelt pattern except for the singularity at  $\theta_1 = 0$ . Some results of convolution in this limiting case are reported in reference (2).

Equation (5) was programmed for numerical evaluation using the conical beam approximation. The singularity at  $\theta_1=0$  was avoided by using small finite initial values. The results for various values of  $u_0=2\alpha R$  are shown in Figures 1 - 3. The scaled conical angle is given by  $\theta_0=\phi_0'/\phi_0$  where  $\phi_0'$  is the half width of the conical beam. The abscissas are the relative angle  $\theta=\phi/\phi_0$  as in reference (1). The ordinates are 20 log10 |Y|. The dotted curve is the Westervelt pattern.

For  $\theta_0$  = 0 the conical beam is a delta function and the pattern has a logarithmic singularity given by  $(u_0 << 1)$ 

$$Y(u_0, v_0) + -u_0 \exp(-u_0) \ln |v_0|$$
  
e + 0 (7)

TM No. 316-489-76

For  $\theta_0 \neq 0$ , Y rapidly approaches the finite axial value for  $\theta < \theta_0$ . For  $\theta_0 > 1$  the curves cross the  $\theta_0 = 0$  curve and approach it from above. For  $\theta_0 \not\rightarrow \infty$  the  $\theta_0 = 0$  curve acts like a delta function with respect to the conical beam. It is clear that only for  $\theta_0 >> 1$  does the actual shape of the source pattern have any significant effect on the result.

Figure 4 compares the results with experiment where  $\theta_0 = 0.4$ . For  $2\alpha L = 1$  the agreement is good. The -3dB beamwidth is only  $\frac{1}{2}$  the Westervelt beamwidth. For  $2\alpha L = 0.25$  the experimental axial value is again roughly 3dB low as it was in the calculations of reference (1). Misalignment of source and receiver is one possible explanation of this error.

#### SATURATION

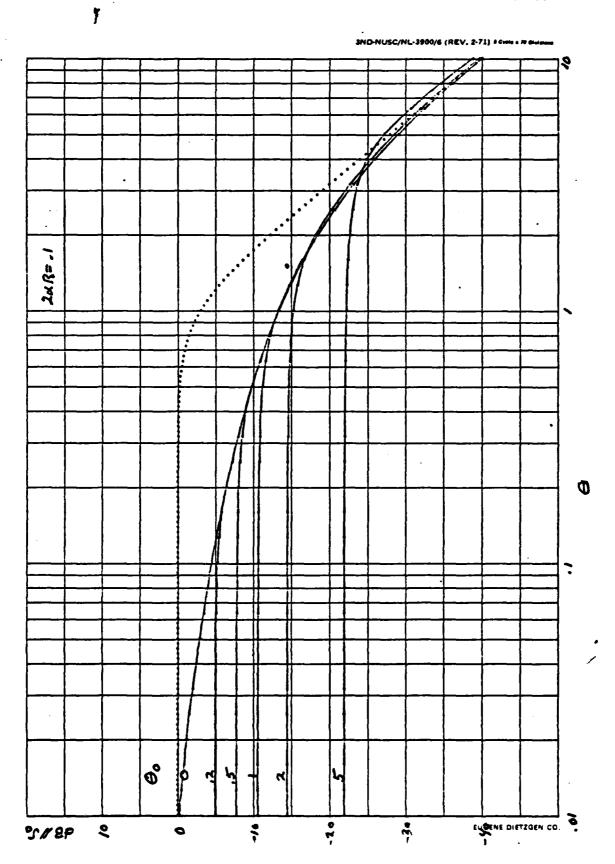
The effects of saturation may be included as in Part II (reference (3)) by multiplying the integrand of Equation (4) by the taper function  $T^2(z)$ . The solution for the cylindrical and spherical cases may also be combined to give a reasonably good approximation for all ranges. At moderate range the spherical part alone should give a sufficiently good approximation if the result is multiplied by the source aperture pattern (reference (4)).

# **REFERENCES**

- 1. R. H. Mellen, "A Nearfield Model of the Parametric Radiator," NUSC Technical Memorandum PA4-230-75, December 1975.
- 2. H. O. Berktay and D. J. Leahy, "Farfield Performance of Parametric Transmitters," J. Acoust. Soc. Am. 55, 539-546 (1974).
- 3. R. H. Mellen, "A Nearfield Model of the Parametric Radiator, Part II: Saturated Sources," NUSC Technical Memorandum PA4-53-76, May 1976.
- 4. M. B. Moffett and R. H. Mellen, "On Parametric Source Aperture Factors," J. Acoust. Soc. Am. 60, 581-583 (1976).

Beam Pattern  $2\alpha R = 0.1$ 

Figure 1.

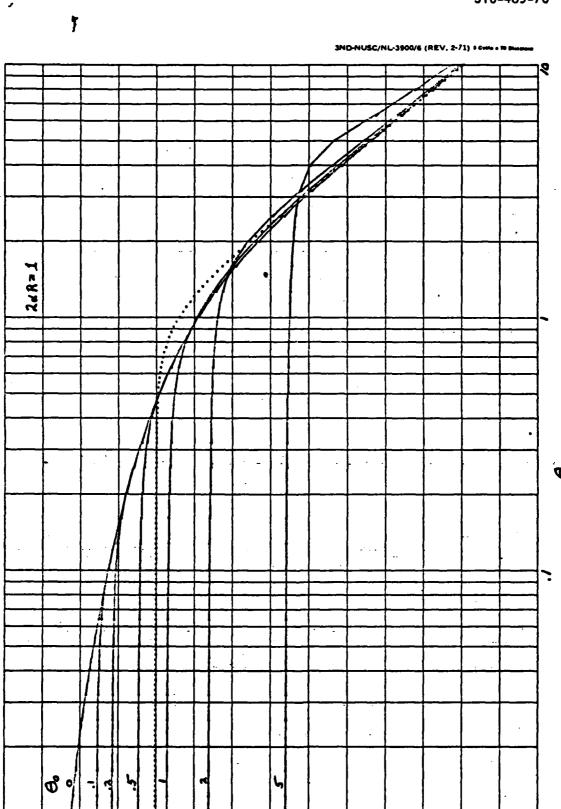


8

Beam Pattern  $2\alpha R = 1$ 

Figure 2.

ESENE DIETZGEN CO.



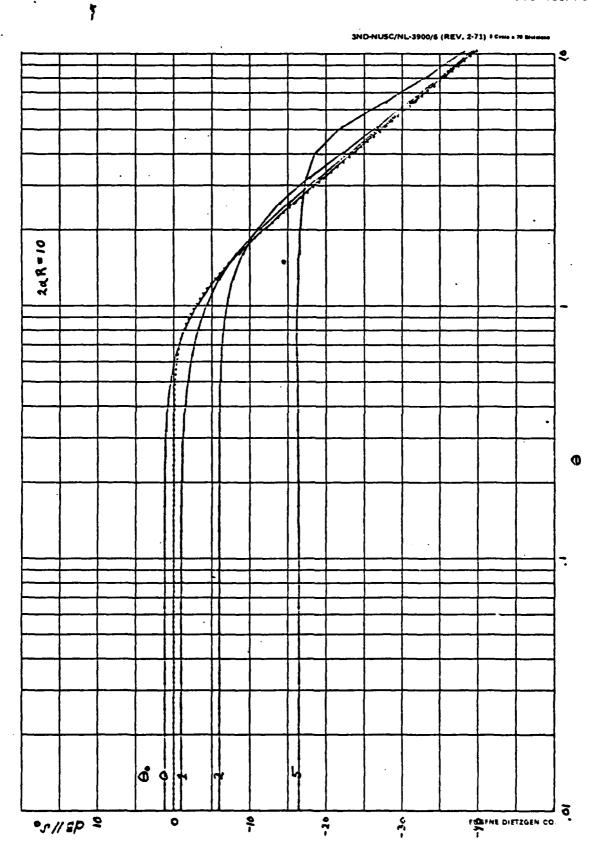
9

°5//8P °

 $2\alpha R = 10$ 

Beam Pattern

Figure 3.



10

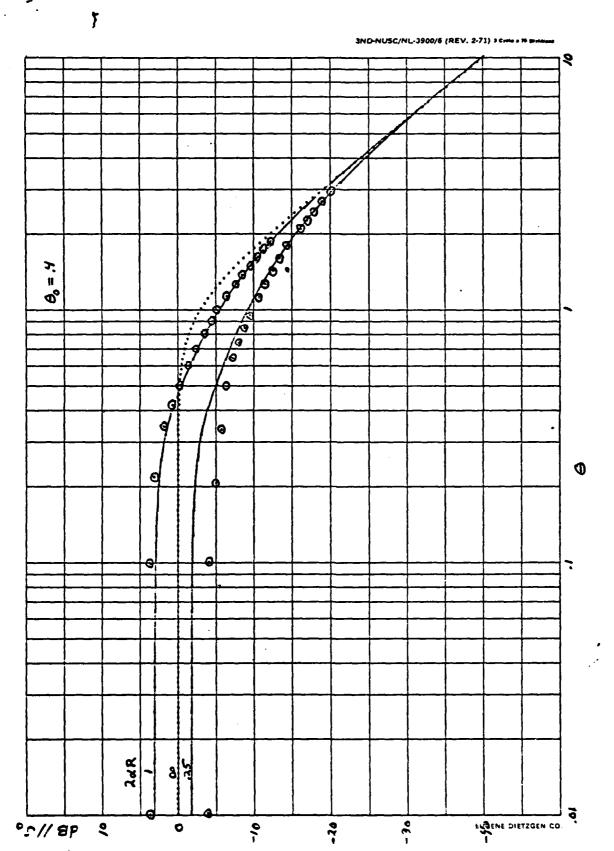


Figure 4. Comparison of experimental and predicted beam patterns.